





## Lesson 3.3.4

3-126. See below:

- How  $f'(x)$  is changing.
- Students give an explanation.

c.

	<b>Increasing or Decreasing?</b>  Walking away from the motion detector? or Walking towards the motion detector?	<b>Concave Up or Concave Down?</b>  Getting faster? or Getting slower?	$f'(x)$	$f''(x)$
	<i>Increasing</i> <i>Away from motion detector</i>	<i>Concave Up</i> <i>Getting faster</i>	<i>Positive</i>	<i>Positive</i>
	[ Decreasing & towards the m.d. ]	[ Concave up & getting slower ]	[ Negative ]	[ Positive ]
	[ Decreasing & towards the m.d. ]	[ Concave down & getting faster ]	[ Negative ]	[ Negative ]
	[ Increasing & away from the m.d. ]	[ Concave down & getting slower ]	[ Positive ]	[ Negative ]

- If the function is increasing, then the slope,  $f'(x)$  is positive. If the function is decreasing, then the slope,  $f'(x)$  is negative. Increasing & Decreasing has NO effect on  $f''(x)$ .
- If the function is concave up, then the slope is increasing,  $f''(x)$  is positive. If the function is concave down, then  $f''(x)$  is negative. The slope of determines concavity  $f'(x)$ .
- no

3-127. Increasing:  $x < -2$  or  $x > 2$ ; Decreasing:  $-2 < x < 2$ ; Concave Up:  $[0, \infty)$ ; Concave Down:  $(-\infty, 0]$

3-128. See below:

- $(0, 0)$

b.  $y'' = 0$

**3-129.** rel max at  $(-2, 20)$ , relative min at  $(2, -12)$ , point of infl:  $(0, 4)$ , inc:  $(-\infty, -2)$  and  $(2, \infty)$ , dec:  $(-2, 2)$ , CD:  $(-\infty, 0)$ , CU:  $(0, \infty)$



**3-131.**  $0, f'(4), \frac{f(3)-f(1)}{3-1}, f'(1)$

**3-132.**  $y = 24z - 19$

**3-133.** Answers should be of the form:  $f(x) = -4x^{3/2} + \cos x + C$ . Students will choose their own constants at this point. They should not be putting "+C" on their answers yet. We will address the "+C" issue in Section 3.4.

**3-134. See below:**

a.  $y'' = 77616x^{97}$

b.  $y'' = \frac{3}{4}x^{3/2}$

c.  $f'' = -36x^{-4}$

d.  $f''(x) = 2 \cos x$

**3-135.**  $f'(x) \geq 0; x \geq 0.5$

**3-136.**  $\approx 20.275; = 20.5; \approx 1\% \text{ error}$

**3-137.** Yes, no

**3-138. See below:**

a.  $y = -\frac{1}{2}$

b.  $y' = -\sin x$

c.  $y' = -2x + 6$

**3-139. See below:**

a. Speed is always positive: 32 meters per second.

b. 36 meters, 64 meters

**3-140. See below:**

- a. 625
- b. 1
- c. 0
- d. DNE but  $y \rightarrow -\infty$