

Lesson 6.4.3

6-150. See below:

- a. $t = 6$ hours, at the end of the trip.
- b. 21 mph
- c. The areas are the same. Both equal 126.
- d. $s(t) = -t^3 + 8.5t^2 + 6t$; $s(6) = 126$, $(126 - 0 \text{ miles}) \div (6 \text{ hrs}) = 21 \text{ mph}$
- e. $t = 1.093$ and $t = 4.573$ hours after he starts; Set answer to part (b) equal to $v(t)$.

6-151. See below:

- a. 11.182 kilowatts; Find area under curve, then divide by 30 days.
- b. During days 15, 17, and 19. Set answer to part (a) equal to $k(t)$.

6-152. The average rate of change of f in $[a, b]$ is zero, so there must be a point c where the instantaneous rate of change is zero.

6-153. $a = -1$ and $b = 1$. $f'(x) = 0$ for $x = -\frac{1}{2}$ and $x = 1$, but only $x = -\frac{1}{2}$ lies in the open interval $(-1, 1)$. Therefore, $c = -\frac{1}{2}$.

6-154. This function is continuous, therefore the Mean Value Theorem applies.

6-155. See below:

- a. Slope of tangents equal the average velocity.
- b. ≈ 3.284 and 11.949 min

6-156. One possible counterexample: $y = \begin{cases} -1 & \text{for } x < 0 \\ 1 & \text{for } x \geq 0 \end{cases}$ over $[-1, 1]$

6-157. 0.464



6-158. See below:

a. $-6x \sin(3x^2)$

b. $-\cos(3x^2) + C$

c. $\frac{27x^8-5}{2\sqrt{3x^9-5x}}$

d. $2\sqrt{3x^9-5x} + C$

6-159. $y = 1.5x^2 + C$

6-160. See below:

a. $K(t) = 8t - \sin t + \frac{0.01}{3}t^3 + \frac{0.01}{2}t^2$; antiderivative or area function

b. $K(30) \approx 335.488$

c. Students sketch graph.

d. Average = 11.183; yes; slope of the line from (0, 0) to (30, 335.488)

6-161. See below:

a. $7\frac{2}{3}$

b. 5.541

6-162. $y = -x + 1$

6-163. Min at $x = -3$, Max at $x = 3$