8.1.3 How can I find the equation?

Ch Ch

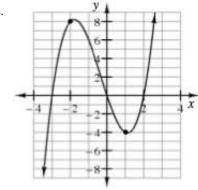
Stretch Factors for Polynomial Functions

In Lesson 8.1.2 you found possible equations for the graphs of polynomial functions based on their x-intercepts. Many of the sketches you used did not even include the scale on the y-axis. In this lesson, you will focus on figuring out equations that represent*all* of the points on the graphs.

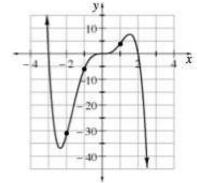
8-45. Find reasonable equations for each of the following polynomial functions. Without using a graphing calculator, how can you check the accuracy of your equations? Were each of your equations accurate? If not, why do you think your equation(s) were not accurate?



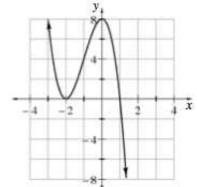
a.



b.

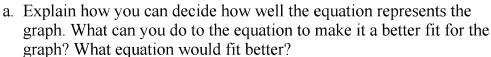


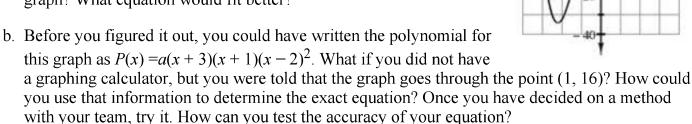
 $\mathbf{c}.$



8-47. ARE THE INTERCEPTS ENOUGH?

Melvin wrote the equation $y = (x + 3)(x + 1)(x - 2)^2$ to represent the graph at right.

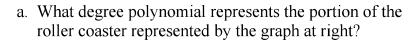




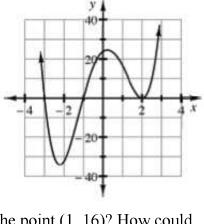


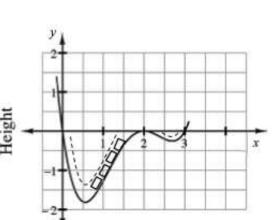
Now that you have more expertise with polynomial equations and their graphs, the Mathamericaland Carnival Company has hired your team to find the *exact* equation to represent its roller-coaster track.

The numbers along the x-axis are in hundreds of feet. At 250 feet, the track will be 20 feet below the surface. This gives the point (2.5, -0.2).

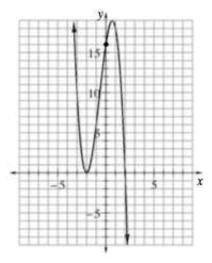


- b. What are the roots?
- c. Find an exact equation for the polynomial that will generate the curve of the track.
- d. What is the deepest point of the roller coaster's tunnel?
- **8-49.** Some polynomials have a stretch factor, just like the a in parabolas and other parent functions. Write an exact equation, including the stretch factor, for each graph below.

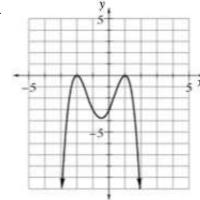




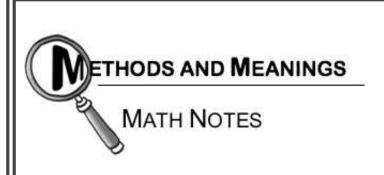
a.



b.



- **8-50.** Write a polynomial equation for a function with a graph that bounces off the *x*-axis at (-1, 0), crosses it at (4, 0), and goes through the point (-2, -18).
- **8-51.** Armando came up with the equation $y = 3(x+1)^4(x-4)$ for problem 8-50. Does his equation fit all of the given criteria? Why or why not? Is it the same as the equation you came up with?
- **8-52.** What if problem 8-50 also had said that the graph went through the point (1, -36)? Is there still more than one possible equation? Explain.
- **8-53.** What information about the graph of a polynomial function is necessary to determine exactly one correct equation? Discuss this with your team.



Notation for Polynomials

The **general equation** of a second-degree (quadratic) polynomial is often written in the form $f(x) = ax^2 + bx + c$, and the general equation of a third-degree (cubic) polynomial is often written in the form $f(x) = ax^3 + bx^2 + cx + d$.

For a polynomial with an undetermined degreen, it is unknown how many letters will be needed for the coefficients. Instead of using a,b,c,d,e, etc., mathematicians use only the letter a, and they used subscripts, as shown below.

$$f(x) = (a_n)x^n + (a_{n-1})x^{(n-1)} + \dots + (a_1)x^1 + a_0$$

This general polynomial has degree n and coefficients a_n , a_{n-1} , ..., a_1 , a_0 .

For example, for $7x^4 - 5x^3 + 3x^2 + 7x + 8$, the degree is 4. In this specific case, a_n is a_4 and $a_4 = 7$, a_{n-1} is $a_3 = -5$, a_{n-2} is $a_2 = 3$, $a_1 = 7$, and $a_0 = 8$.



- **8-54.** What is the stretch factor for the equation of the graph in part (c) of problem 8-45? Write the exact equation of the function. Homework Help €
- **8-55.** For each of the following polynomial expressions, find the degree, list the coefficients, and then label them a_0 through a_n . Refer to the example in the Math Notes box above about polynomial notation.

Homework Help **№**

a.
$$6x^4 - 3x^3 + 5x^2 + x + 8$$

b.
$$-5x^3 + 10x^2 + 8$$

c.
$$-x^2 + x$$

d.
$$x(x-3)(x-5)$$

- e. *x*
- f. 10
- **8-56.** Write a polynomial equation for a graph that passes through the point (-1, 60) and has three *x*-intercepts: (-4, 0), (1, 0), and (3, 0). Homework Help

a.
$$x = \frac{3}{4}, x = -2$$

b.
$$x = -\sqrt{5}, x = \sqrt{5}$$

8-58. Solve the equation $\sqrt{5-2x}+7=4$ and check your solution. Homework Help

8-59. Find the center and radius of each circle below. Homework Help **№**

a.
$$(y-7)^2 = 25 - (x-3)^2$$

b.
$$x^2 + y^2 + 10y = -9$$

c.
$$x^2 + y^2 + 18x - 8y + 47 = 0$$

d.
$$v^2 + (x-3)^2 = 1$$

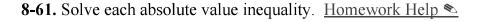
8-60. Without using a calculator, find the solution to each equation. Homework Help **№**

a.
$$2^x = 17$$

b.
$$\log_3(x+1) = 5$$

c.
$$\log_3(3^x) = 4$$

d.
$$4^{\log_4(x)} = 7$$



a.
$$|2x+1| < 5$$

b.
$$2|3x-2| \ge 10$$

8-62. Write a possible equation for the graph below. Homework Help

